

Electrical Technology

Contents

Start - Delta Transformation

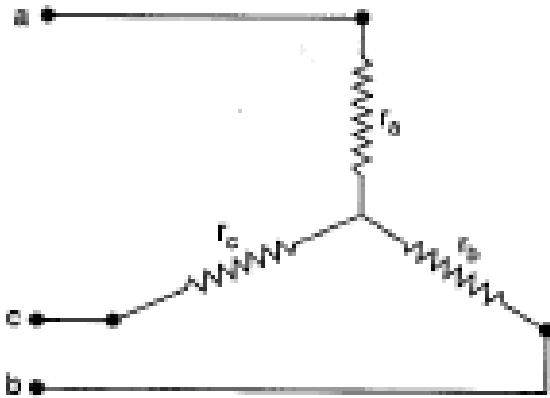
Delta – Star Transformation

Test Yourself

NPTEL Link

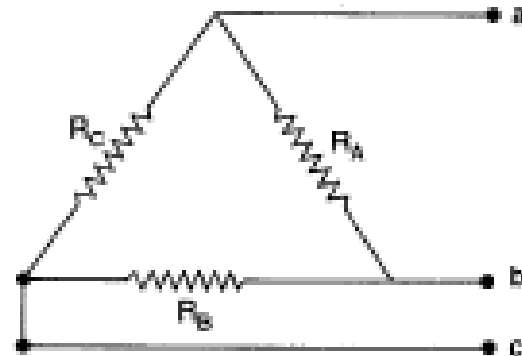
Start Delta Transformation

Given Star

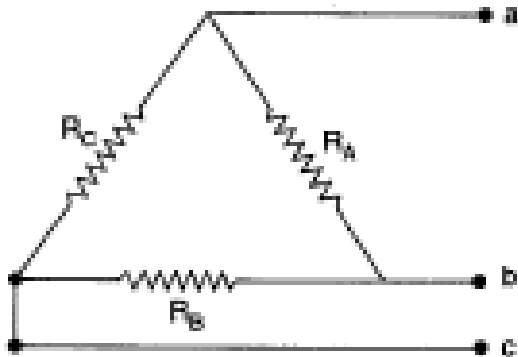


Star to
Delta

Determine Equivalent Delta

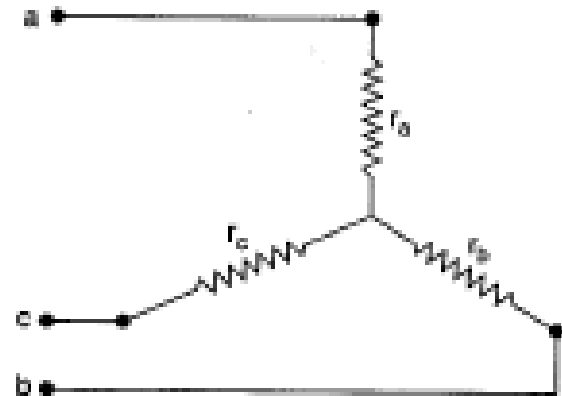


Given Delta



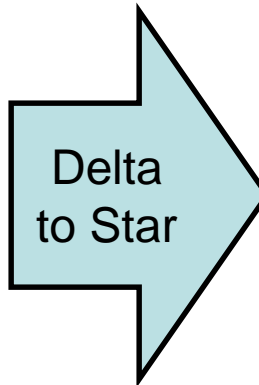
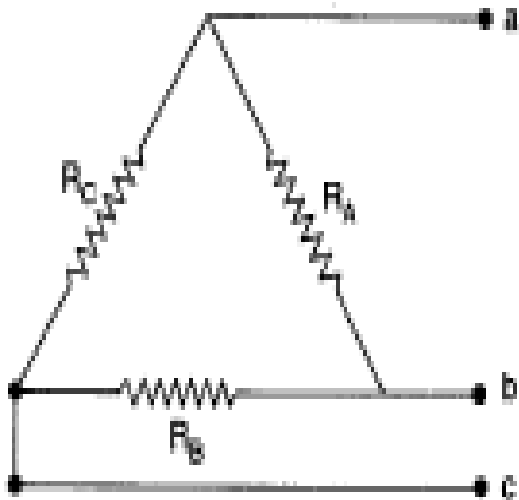
Delta to
Star

Determine Equivalent Star

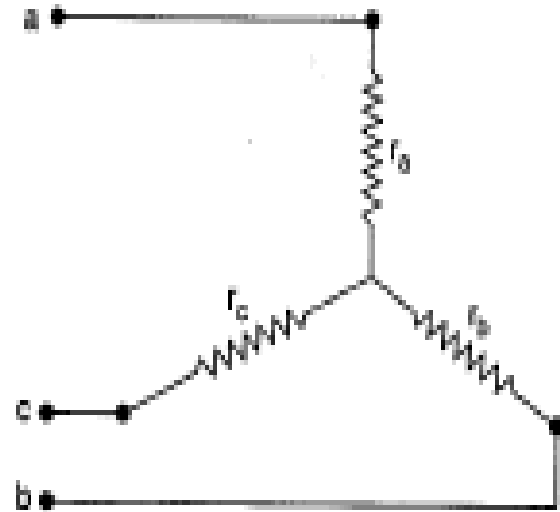


Start Delta Transformation

Given Delta



Determine Equivalent Star



- In Delta connection Resistance between terminals 1 and 2

$$= R_{12} \times (R_{23} + R_{31}) / [R_{12} + (R_{23} + R_{31})]$$

$$= R_{12} \times (R_{23} + R_{31}) / [R_{12} + R_{23} + R_{31}]$$

In Star connection Resistance between terminals 1 and 2

$(R_1 + R_2)$. As terminal resistances have to be same

$$(R_1 + R_2) = R_{12} \times (R_{23} + R_{31}) / [R_{12} + R_{23} + R_{31}] \quad (i)$$

Similarly for terminals 2 and 3 and terminals 3 and 1 , we have

$$R_2 + R_3 = R_{23} \times (R_{31} + R_{12}) / [R_{12} + R_{23} + R_{31}] \quad (ii)$$

$$R_3 + R_1 = R_{31} \times (R_{12} + R_{23}) / [R_{12} + R_{23} + R_{31}] \quad (iii)$$

Subtracting (ii) from (iii) and adding to (i) we get

Delta to star conversions

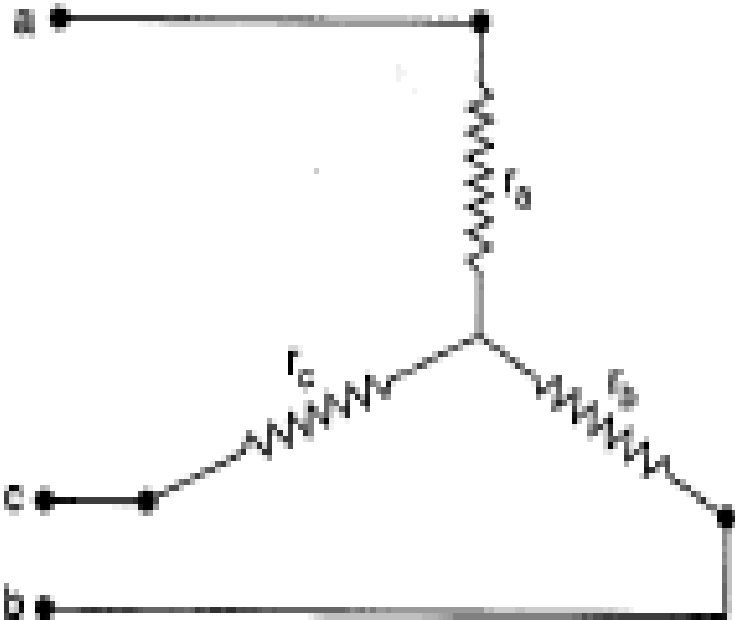
$$R_1 = (R_{12} \times R_{31}) / [R_{12} + R_{23} + R_{31}] . \quad (iv)$$

Similarly we have

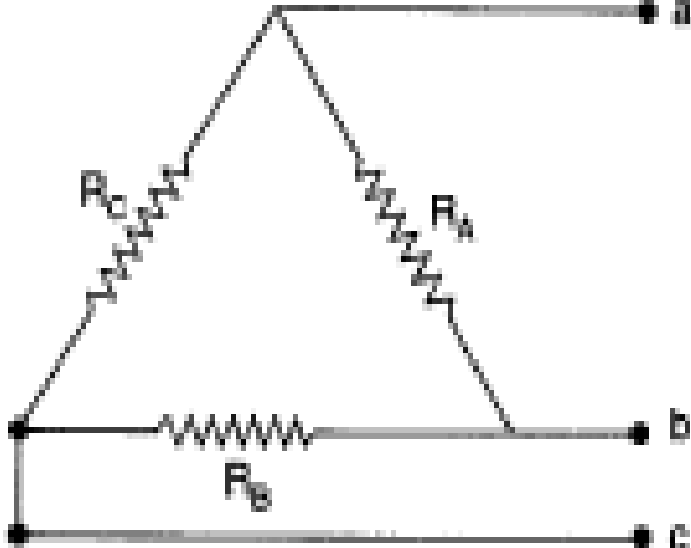
$$R_2 = (R_{23} \times R_{12}) / [R_{12} + R_{23} + R_{31}] \text{ and} \quad (v)$$

$$R_3 = (R_{31} \times R_{23}) / [R_{12} + R_{23} + R_{31}] \quad (vi)$$

Star- Delta Transformation



(a)



(b)

Delta to star conversions we have

$$R_1 = (R_{12} \times R_{31}) / [R_{12} + R_{23} + R_{31}] \quad (\text{iv})$$

$$R_2 = (R_{23} \times R_{12}) / [R_{12} + R_{23} + R_{31}] \text{ and} \quad (\text{v})$$

$$R_3 = (R_{31} \times R_{23}) / [R_{12} + R_{23} + R_{31}] \quad (\text{vi})$$

For Star to Delta Conversion

Multiply (iv) by (v) , (v) by (vi) and (vi) by (iv) and adding

$$\bullet R_1 R_2 + R_2 R_3 + R_3 R_1 = (R_{12} R_{23} R_{31}) / [R_{12} + R_{23} + R_{31}] \quad (\text{vii})$$

• Dividing (vii) by (iv)

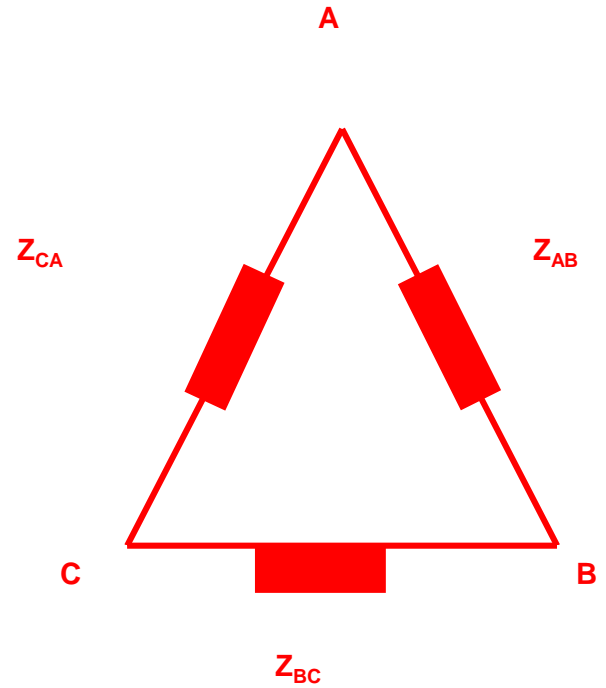
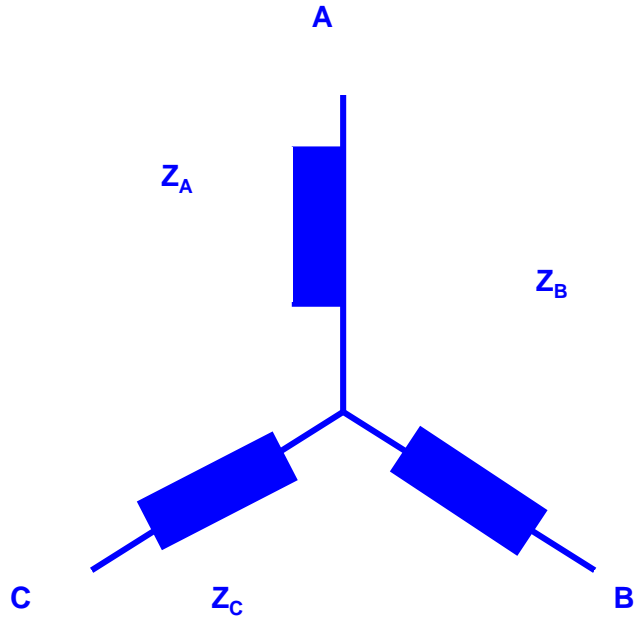
$$\bullet \text{ We have } R_{23} = R_2 + R_3 + (R_2 R_3) / R_1 \quad (\text{viii})$$

• Similarly we have

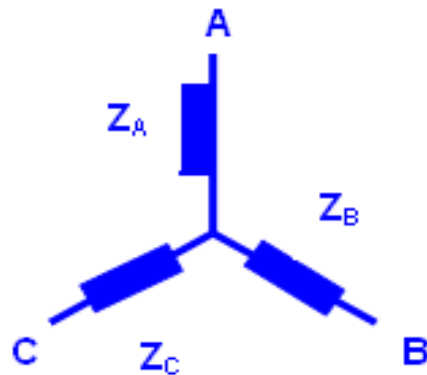
$$\bullet R_{31} = R_3 + R_1 + (R_3 R_1) / R_2 \quad (\text{ix})$$

$$\bullet R_{12} = R_1 + R_2 + (R_1 R_2) / R_3$$

STAR DELTA TRANSFORMATION



STAR

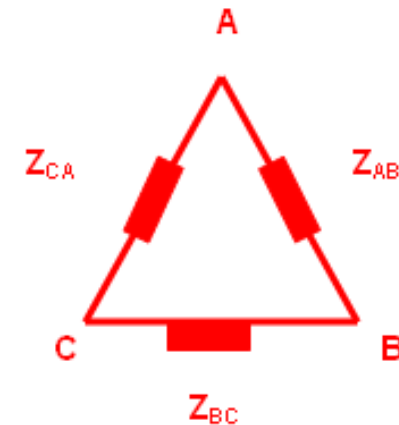
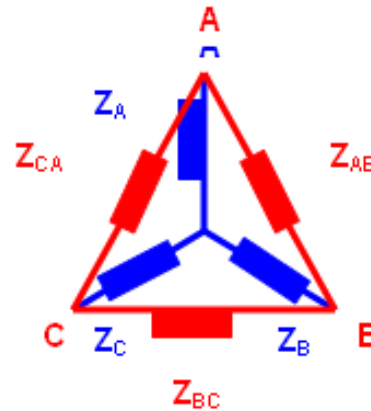


$$Z_A = \frac{Z_{AB}Z_{AC}}{Z_{AB} + Z_{BC} + Z_{CA}}$$

$$Z_B = \frac{Z_{BC}Z_{AB}}{Z_{AB} + Z_{BC} + Z_{CA}}$$

$$Z_C = \frac{Z_{CA}Z_{BC}}{Z_{AB} + Z_{BC} + Z_{CA}}$$

DELTA

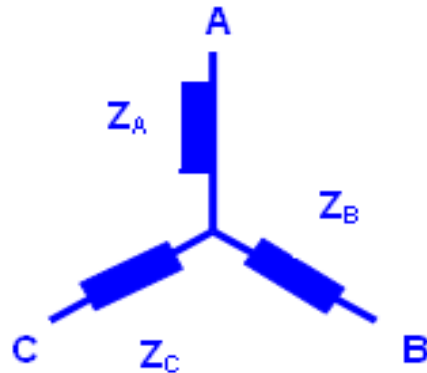


$$Z_{AB} = \frac{Z_A Z_B + Z_B Z_C + Z_C Z_A}{Z_C}$$

$$Z_{BC} = \frac{Z_A Z_B + Z_B Z_C + Z_C Z_A}{Z_A}$$

$$Z_{CA} = \frac{Z_A Z_B + Z_B Z_C + Z_C Z_A}{Z_B}$$

STAR

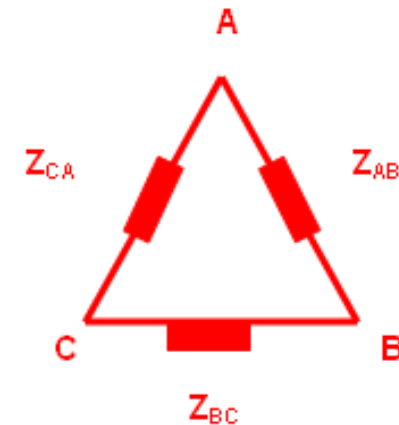
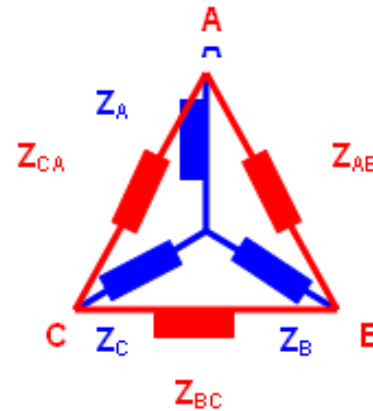


$$Z_A = \frac{Z_{AB}Z_{AC}}{Z_{AB} + Z_{BC} + Z_{CA}}$$

$$Z_B = \frac{Z_{BC}Z_{AB}}{Z_{AB} + Z_{BC} + Z_{CA}}$$

$$Z_C = \frac{Z_{CA}Z_{CB}}{Z_{AB} + Z_{BC} + Z_{CA}}$$

DELTA



$$Z_{AB} = \frac{Z_A Z_B + Z_B Z_C + Z_C Z_A}{Z_C}$$

$$Z_{BC} = \frac{Z_A Z_B + Z_B Z_C + Z_C Z_A}{Z_A}$$

$$Z_{CA} = \frac{Z_A Z_B + Z_B Z_C + Z_C Z_A}{Z_B}$$